

### **Parameterize Turbulent Surface Flux**

#### Momentum Flux:

$$\tau \equiv -\rho \overline{uw} = \rho u_*^2 = \rho C_{Dr} S_r^2$$

Sensible Heat Flux:

$$H_{s} \equiv \rho c_{p} \overline{wt} = \rho c_{p} C_{Hr} S_{r} (T_{s} - T_{r})$$

Latent Heat Flux:

$$H_L \equiv \rho L_v \overline{wq} = \rho L_v C_{Er} S_r (Q_s - Q_r)$$



## **Drag Coefficient**

$$C_{Dr} = \frac{k^2}{\left[ln(r/z_0) - \psi_m(r/L)\right]^2}$$

where k is the von Kármán constant, r is an arbitrary reference height,  $z_0$  is the roughness length for momentum, L is the Obukhov length, and  $\psi_m$  is a stability correction

#### **Scalar Transfer Coefficients**

#### For Sensible Heat:

$$C_{Hr} = \frac{k^2}{\left[\ln\left(\frac{r}{z_0}\right) - \psi_m\left(\frac{r}{L}\right)\right] \left[\ln\left(\frac{r}{z_T}\right) - \psi_h\left(\frac{r}{L}\right)\right]}$$

For Latent Heat:

$$C_{Er} = \frac{k^2}{\left[\ln\left(\frac{r}{z_0}\right) - \psi_m\left(\frac{r}{L}\right)\right] \left[\ln\left(\frac{r}{z_Q}\right) - \psi_h\left(\frac{r}{L}\right)\right]}$$

### **Drag Coefficient: 10m, Neutral**

In neutral stratification, at a standard reference height of 10 m,

$$C_{DN10} = \frac{k^2}{\left[\ln(10/z_0)\right]^2}$$

where

$$z_{_{0}}\,=\,r\,exp\Bigl\{-\Bigl[k\,C_{_{D}r}^{_{-1/2}}\,+\,\psi_{_{m}}\bigl(r\,/\,L\bigr)\Bigr]\Bigr\}$$

### Scalar Transfer Coefficients: Neutral

In neutral stratification, at a standard reference height of 10 m, the scalar transfer coefficients are

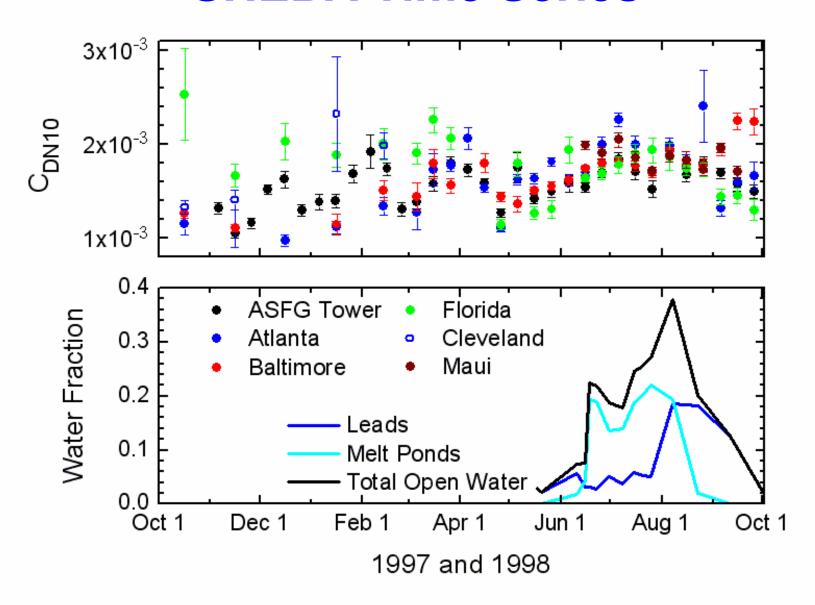
$$C_{sN10} = \frac{k^2}{[ln(10/z_0)][ln(10/z_s)]} = \frac{kC_{DN10}^{1/2}}{ln(10/z_s)}$$

where

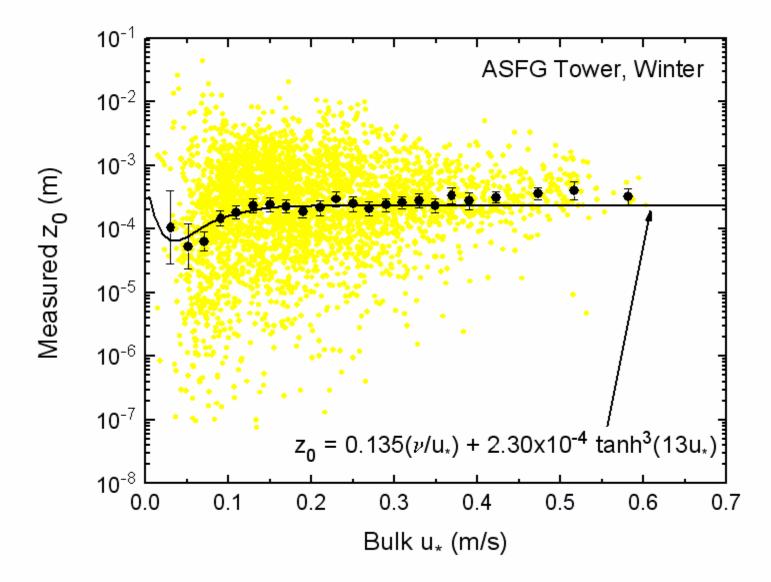
$$z_{s} = r exp \left\{ - \left\lceil k C_{Dr}^{1/2} C_{sr}^{-1} + \psi_{h} \left( r/L \right) \right\rceil \right\}$$

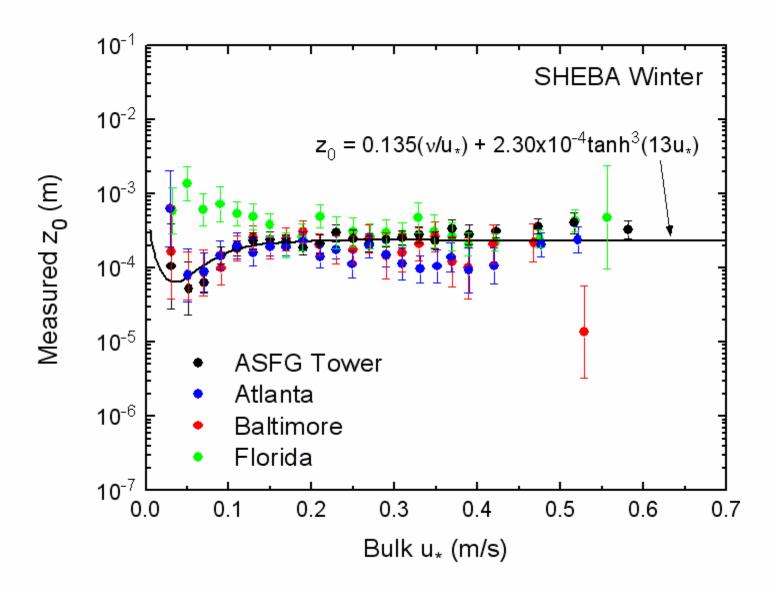


### **SHEBA Time Series**

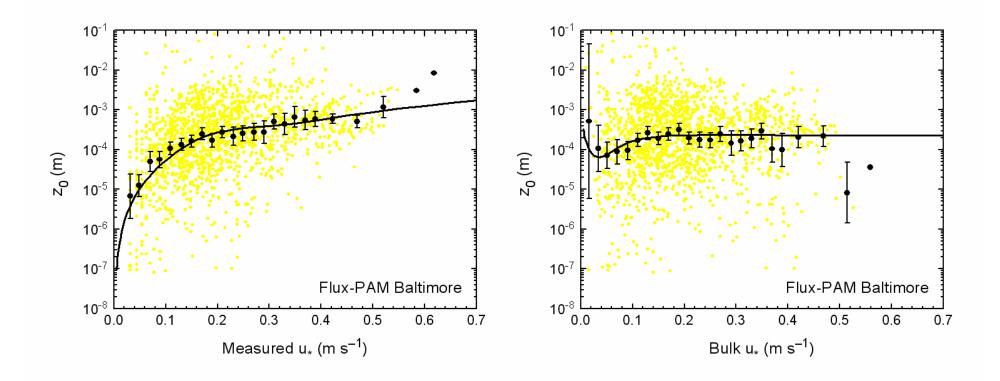






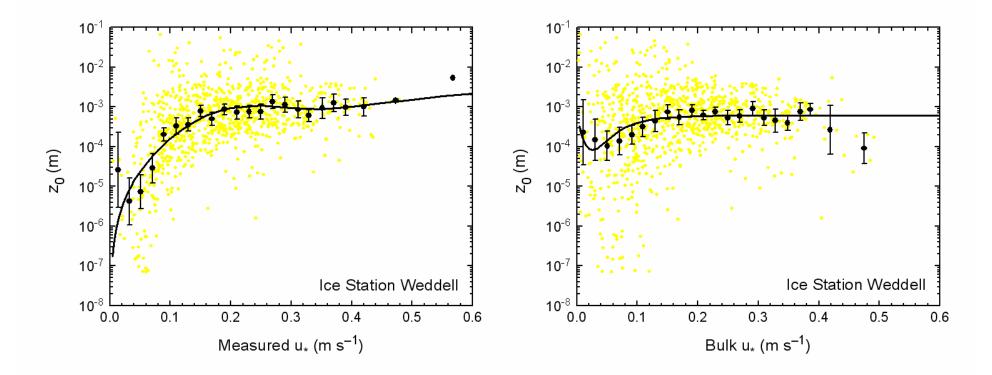


### **Effect of Fictitious Correlation**



**Example from SHEBA** 

## **Effect of Fictitious Correlation, #2**



Example from Ice Station Weddell

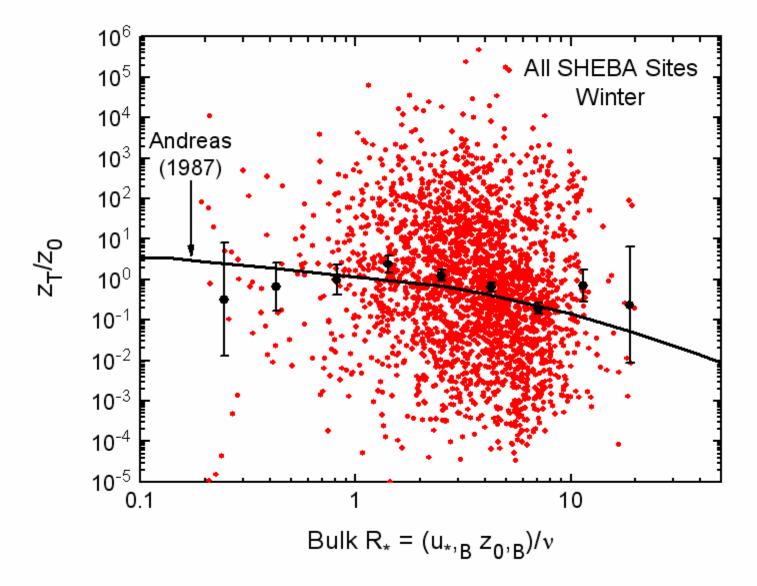
### Why the Fictitious Correlation?

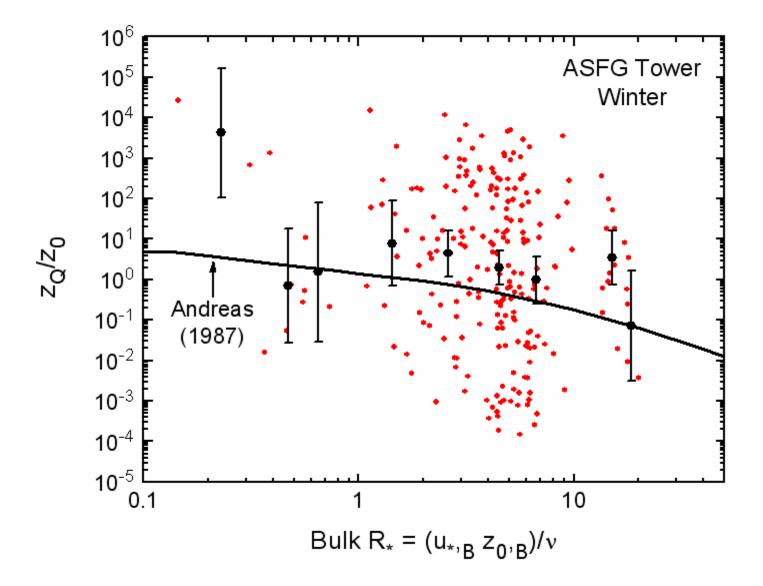
In plots of measured  $z_0$  versus measured  $u_*$ ,  $z_0$  comes from

$$z_0 = r exp \left\{ -\left[ \frac{k S_r}{u_*} + \psi_m(r/L) \right] \right\}$$

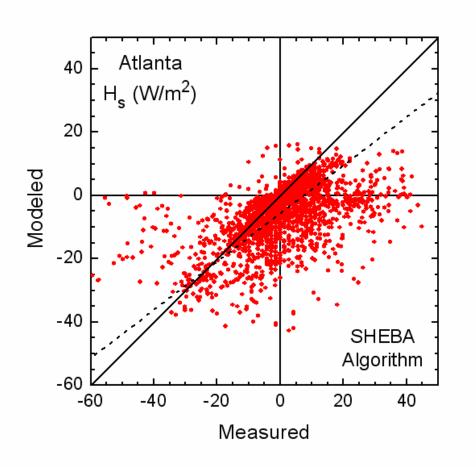
where also

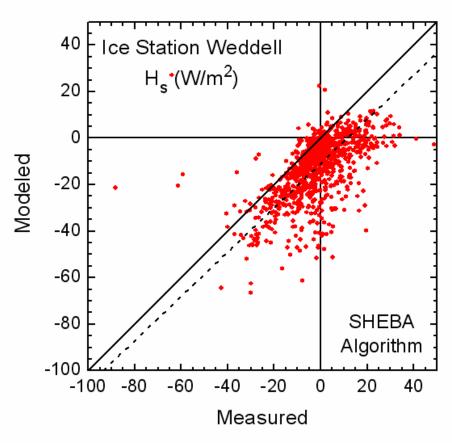
$$\frac{r}{L} = -\frac{k g r}{T u_{\star}^3} \left( \frac{H_s}{\rho c_p} + \frac{0.61T}{1 + 0.61Q} \frac{H_L}{\rho L_v} \right)$$



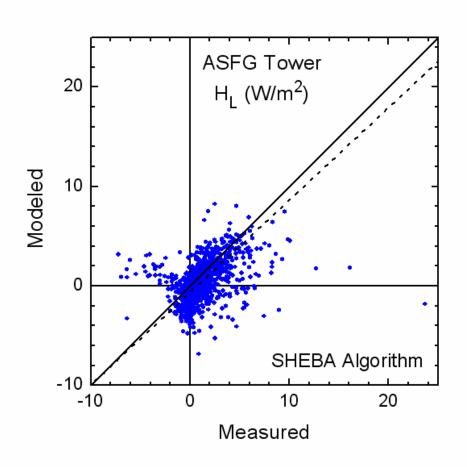


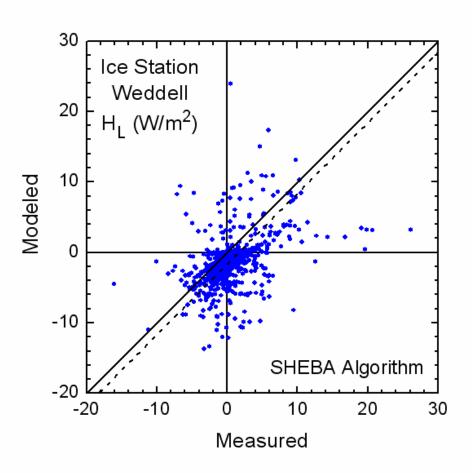
### **Sensible Heat Flux**



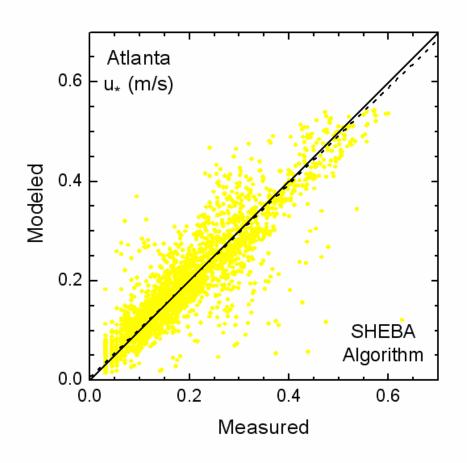


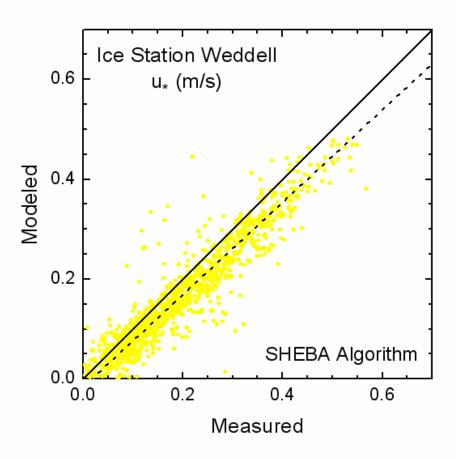
### **Latent Heat Flux**



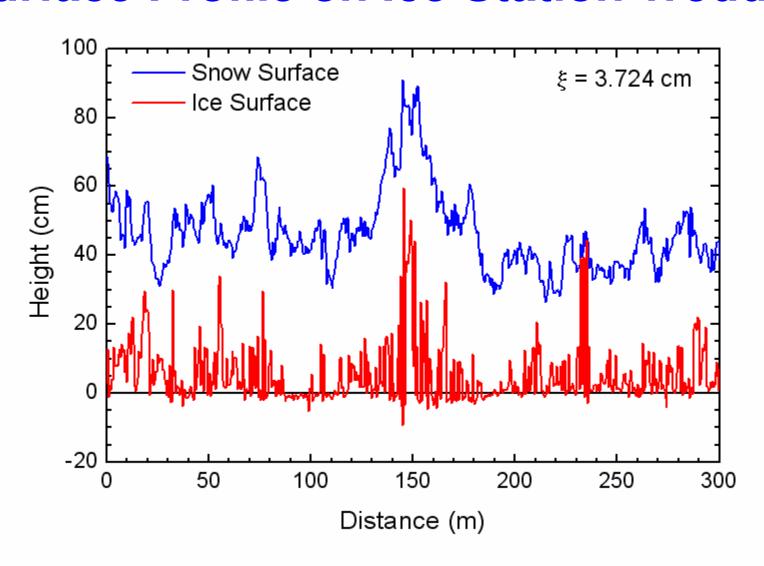


# **Friction Velocity**





### Surface Profile on Ice Station Weddell



## **Quantify Physical Roughness**

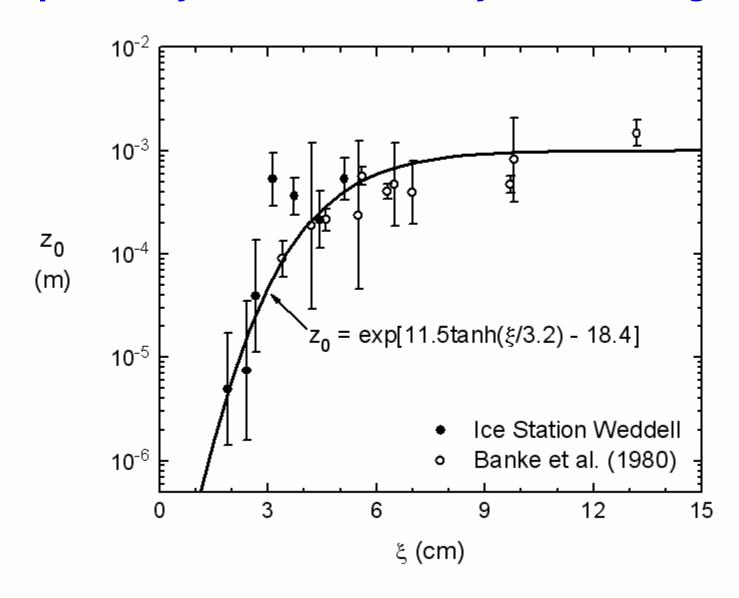
A roughness parameter related to the surface variance (from Banke et al. 1980)

$$\xi^2 = \int_{\kappa_0}^{\infty} \Phi(\kappa) d\kappa$$

where  $\kappa$  is the wavenumber, and  $\Phi(\kappa)$  is the wavenumber spectrum of the surface elevation

 $\kappa_0$  is a cutoff wavenumber of 0.5 rad m<sup>-1</sup> (equivalent to a maximum wavelength of 12.6 m)

#### **Compare Physical and Aerodynamic Roughness**



### What a Turbulent Flux Algorithm Does

- It's a "Flux Coupler."
- It provides estimates of the surface fluxes of momentum and sensible and latent heat from measured or modeled meteorological quantities (wind speed, surface temperature, air temperature, humidity).
- It provides the lower flux boundary conditions for the atmosphere.
- It provides the upper flux boundary conditions for the ice or ocean.



Dramatic pause . . .

# **Discussion, Topic 1**

Does anyone besides turbulence aficionados like me really care about the turbulent surface fluxes over sea ice?

### Discussion, Topic 2

What accuracy should we strive for in measuring, parameterizing, and modeling the surface fluxes (including now the radiative fluxes)?

For example, the TOGA COARE program (tropical Pacific Ocean) aimed for an uncertainty of ±10 W m<sup>-2</sup> in the surface energy budget.

### **Discussion, Topic 3**

Do we know enough yet and would there be any value in compiling gridded datasets of surface fluxes for the Arctic and Antarctic sea ice regions, as is being done over the global wet ocean?

A catch is that the ocean sets benefit from buoys, ships of opportunity, and satellite-derived surface winds.